

(a) We are looking for voltages, but many current sources are given \therefore use the Mesh method. We are given all the mesh currents!

$$\begin{aligned} i_1 &= 9A \\ i_2 &= 16A \\ i_3 &= 14A \\ i_4 &= 6A \end{aligned}$$

Now, add or subtract mesh currents to obtain branch currents and use the definition of voltage, i.e. potential difference, to find node voltages, e.g. $V_A = V_{AG} = V_{AD} + V_{DE} + V_{EG}$ or $V_A = V_{AD} + V_{DG}$.

$$\text{Step 1: } i_x = i_2 - i_4 = 10A \Rightarrow V_E = V_{EG} = 7.5i_x = 75V$$

$$\begin{aligned} \text{Step 2: } V_D &= V_{DE} + V_{EG} = V_{DE} + V_E = (i_3 - i_1) \times 4\Omega + V_E \\ &= V_{DG} &= 5 \times 4V + 75V = 280V \end{aligned}$$

$$\text{Step 3: } V_A = V_{AD} + V_{DG} = -i_1 \times 20\Omega + V_{DG} = -9 \times 20 + 280 = \underline{100V}$$

$$\text{Step 4: } V_B = V_{BE} + V_{EG} = (i_1 + i_2) \times 5\Omega + V_{EG} = 25 \times 5 + 75 = \underline{200V}$$

$$\text{Also, for practice: } V_F = (i_4 - i_2) \times 3.5 + V_E = -10 \times 3.5 + 75 = 40V$$

$$V_C = -i_2 \times 15 + V_F = -16 \times 15 + 40 = -200V$$

In summary, we have found all node voltages relative to the ground node, G : $V_A = 100V$, $V_B = 200V$, $V_C = -200V$, $V_D = 280V$, $V_E = 75V$, $V_F = 40V$.

$$\begin{aligned} \text{(b) } V_{BA} &= V_B - V_A = 200 - 100 = 100V \\ V_{BA} \times i_1 &= 100 \times 9 = 900W \end{aligned} \quad \left. \begin{array}{l} \text{since } i_1 \text{ leaves the positive} \\ \text{node of } V_{BA}, \text{ power is generated.} \end{array} \right\}$$

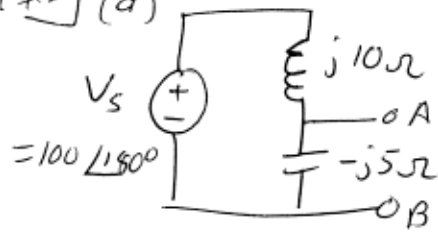
$$\text{or: } P_{\text{active}} = V_{BA} \times i_1 \quad \left[\text{active notation } \begin{array}{c} - \\ \boxed{V_{BA}} \\ + \end{array} \rightarrow i_1 \right]$$

$$= 900W > 0 \therefore \text{generated.}$$

$$\text{or: } P_{\text{passive}} = V_{AB} \times i_1 \quad \left[\text{passive notation } \begin{array}{c} \rightarrow i_1 \\ \boxed{V_{AB}} \\ - \end{array} \right]$$

$$= -100V \times 9A = -900W < 0 \therefore \text{generated.}$$

#2 (a)



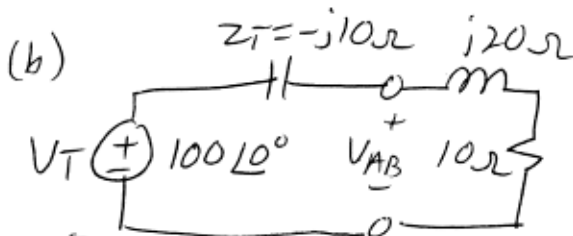
$$V_T = V_{AB} \text{ open circuit} \quad \leftarrow \Rightarrow 100 \angle 180^\circ$$

$$= \frac{-j5}{j10 - j5} \times (-100V)$$

A voltage division factor

$$= -\frac{1}{2} \times -100V = \underline{100 \angle 0^\circ V}$$

Now let $V_s = 0 \Rightarrow Z_T = -j5 \parallel j10 = \frac{-j5 \times j10}{j5} = \frac{50}{j5} = \underline{-j10 \Omega}$



step ②

$$I_0 = \frac{V_T}{-j10 + j20 + 10} \quad \text{or} \quad \frac{V_{AB}}{10 + j20} \quad \leftarrow \text{use (*)}$$

$$= \frac{100}{10 + j10}$$

$$= \frac{10}{\sqrt{2}} \angle -45^\circ \text{ A}$$

step ①

$$V_{AB} = 100V \times \frac{10 + j20}{10 + j20 - j10} = 100 \times \frac{10 + j20}{10 + j10} \quad (*)$$

$$= 100 \times \frac{\sqrt{5} \angle 63^\circ}{\sqrt{2} \angle 45^\circ} = 158 \angle 18^\circ \text{ V}$$

A $\frac{110 + j20}{110 + j10} = \frac{11 + j2}{11 + j1} = \frac{\sqrt{1^2 + 2^2}}{\sqrt{1^2 + 1^2}}$

$$= 158 \angle 18^\circ \text{ V}$$

$$\Rightarrow V_{AB}(t) = 158 \cos(\omega t + 18^\circ) \text{ V}$$

where $\omega = 2\pi 60 = 377 \text{ rad/s}$

$$\Rightarrow I_0(t) = 7.07 \cos(\omega t - 45^\circ) \text{ A}, \quad \omega = 377 \text{ rad/s}$$

$$P_{out} = \frac{|V_{AB}|}{\sqrt{2}} \times \frac{|I_0|}{\sqrt{2}} \cos(\theta_{V_{AB}} - \theta_{I_0})$$

$$= \frac{158}{\sqrt{2}} \times 5 \cos 63^\circ$$

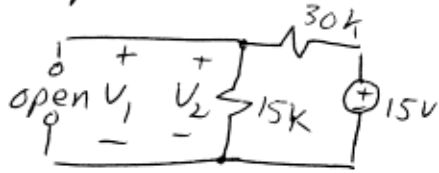
$$= \underline{250 \text{ W}}$$

or $P_{out} = I_{0rms}^2 \times R = 5^2 \times 10 = \underline{250 \text{ W}}$

$P_{avg} = 0$ since an inductor does not dissipate energy.

#3 First note: $\frac{1}{3\mu F} + \frac{1}{5\mu F} = \frac{1}{8\mu F} \Rightarrow \frac{1}{8\mu F} \Rightarrow \frac{1}{4\mu F}$

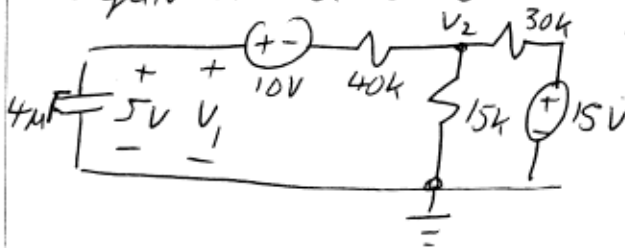
Equiv Circuit at $t=0^-$



$$V_1(0^-) = \frac{15k}{15k+30k} \times 15V = \boxed{5V}$$

$$V_2(0^-) = V_1(0^-) = \boxed{5V}$$

Equiv Circ at $t=0^+$



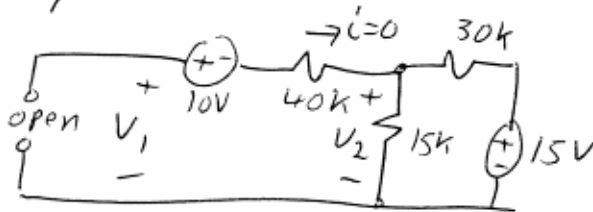
Note: $V_{cap}(0^+) = V_{cap}(0^-) \Rightarrow V_1(0^+) = \boxed{5V}$

Find $V_2(0^+)$. Let's use Node Method

$$\frac{V_2 - (5V - 10V)}{40k} + \frac{V_2}{15k} + \frac{V_2 - 15V}{30k} = 0$$

$$\Rightarrow \underline{V_2(0^+) = \boxed{3V}}$$

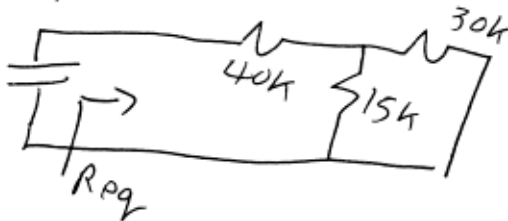
Equiv Circ at $t=\infty$



$$V_2(\infty) = \frac{15k}{45k} \times 15V = \boxed{5V}$$

$$V_1(\infty) = V_2(\infty) + i \times 40k + 10V = \boxed{15V}$$

Equiv Circ at $t > 0$ with sources set to zero:



The resistance "seen" by the capacitor is

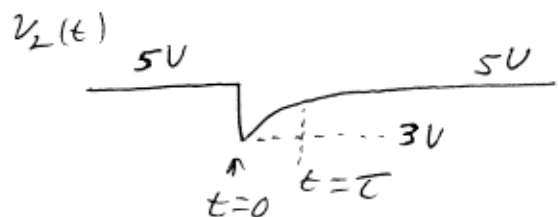
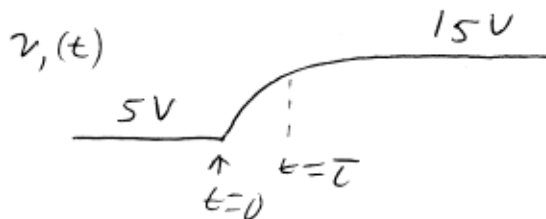
$$R_{eq} = 40k + 15k // 30k = 40k + 10k = 50k\Omega$$

$$\therefore \tau = R_{eq} C_{eq} = 50k \times 4\mu = \underline{200ms}$$

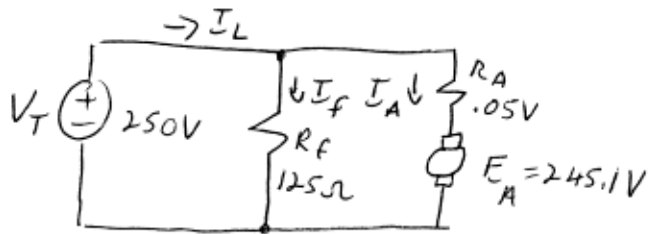
For graphs note $V(0^-)$, $V(0^+)$, $V(\infty)$

V_1 : 5V, 5V, 15V

V_2 : 5V, 3V, 5V

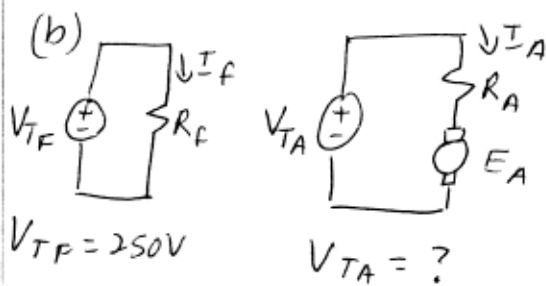


#4 (a) DC steady state Model
Note: $V_{\text{inductor}} = 0$



$$n_{\text{rated}} = 4500 \text{ rpm} \Rightarrow \omega_{\text{rated}} = 2\pi \times \frac{4500}{60} = 471.24 \frac{\text{rad}}{\text{s}}$$

$$P_{\text{out}} = P_{\text{motor}} = 30 \text{ HP} = 30 \text{ HP} \times \frac{746 \text{ W}}{\text{HP}} = 22380 \text{ W}$$



$$V_{TF} = 250 \text{ V}$$

$$V_{TA} = ?$$

I_f still 2A \therefore $k\phi$ same as in part (a)

$$\therefore E_A \propto \omega \Rightarrow E_A = \frac{1500 \text{ rpm}}{4500 \text{ rpm}} \times 245.1 \text{ V} = 81.7 \text{ V}$$

Since $T_{\text{out}} = \text{const}$

$$\Rightarrow P_{\text{out}} = \frac{1500}{4500} P_{\text{rated}} = \frac{1}{3} \times 10 \text{ HP} = 7460 \text{ W}$$

$$\text{But } E_A I_A = P_{\text{out}} + P_{\text{fric}} \xrightarrow{\text{given } \approx 0}$$

$$81.1 \times I_A = 7460 \text{ W} \Rightarrow I_A = \cancel{4.6 \text{ A}} 91.3 \text{ A}$$

$$\therefore V_{TA} = E_A + I_A R_A = 81.7 \text{ V} + 91.3 \times 0.05 = 81.7 \text{ V} + 4.6 \text{ V} = 86.3 \text{ V}$$

From (a)

$$\text{* Alternative way: } E_A = k\phi \omega \Rightarrow k\phi = \frac{E_A}{\omega} = \frac{245.1}{471.24} = 0.5201$$

$$\therefore \text{For (b) } E_A = k\phi \times \omega = 0.5201 \times 2\pi \left(\frac{1500}{60}\right) = 81.7 \text{ V}$$

(a) cont'd

$$I_f = \frac{250 \text{ V}}{125 \Omega} = 2 \text{ A}$$

$$I_A = \frac{250 \text{ V} - 245.1 \text{ V}}{0.05 \Omega} = 98 \text{ A}$$

$$\therefore I_L = I_f + I_A = 100 \text{ A}$$

$$P = T\omega \Rightarrow T_{\text{out}} = \frac{P_{\text{out}}}{\omega} = \frac{22380 \text{ W}}{471.24 \frac{\text{rad}}{\text{s}}} = 47.49 \text{ Nm}$$

$$\text{Field loss} = I_f^2 R_f = 500 \text{ W}$$

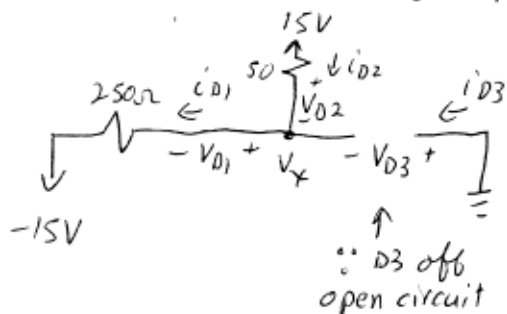
$$\text{Arm loss} = I_A^2 R_A = 480.2 \text{ W}$$

$$E_A I_A = P_{\text{out}} + P_{\text{fric}}$$

$$\therefore P_{\text{fric}} = E_A I_A - P_{\text{out}} = 245.1 \times 98 - 22380 = 1640 \text{ W}$$

$$\eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{22380}{250 \times 100} = 89.52\%$$

#5 By the method of assumed states (ie trial and error) we determine that we have D1 on, D2 on, D3 off:



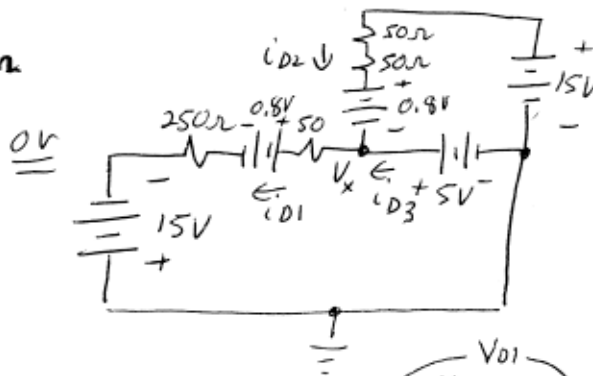
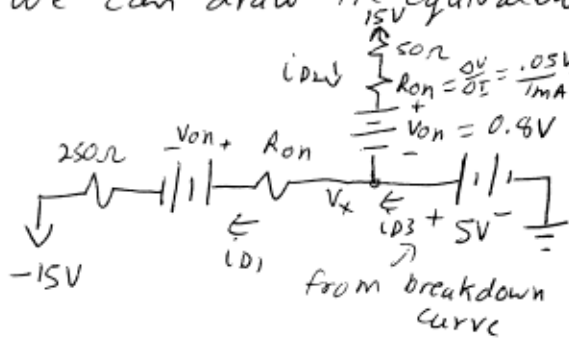
$i_{D3} = 0$

let $i = i_{D1} = i_{D2} = \frac{V_{total}}{R_{total}} = \frac{30V}{300\Omega} = 100mA$

$V_{D1} = V_{D2} = 0$

$V_x = -15V + i \times 250 = 10V \Rightarrow V_{D3} = -10V$

(b) Now assume D1 on, D2 on, D3 in breakdown: We can draw the equivalent circuit many ways. Here are 2 ways:



Using either of these circuits:

$i_{D1} = \frac{15V + V_x - V_{on}}{250 + R_{on}} = \frac{15 + 5 - 0.8}{300} = 64mA$

$i_{D2} = \frac{-V_{on} - 5V + 15V}{50 + R_{on}} = \frac{-0.8 - 5 + 15}{100} = 92mA$

By KCL

$i_{D3} = i_{D1} - i_{D2} = 64mA - 92mA = -28mA$

Note: $1mA = 0.001A = 10^{-3}A$

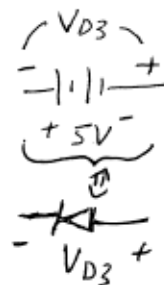
Noting on diode \Rightarrow

$V_{D1} = V_{on} + i_{D1} R_{on} = 0.8V + 0.064 \times 50 = 0.8 + 3.2V = 4.0V$

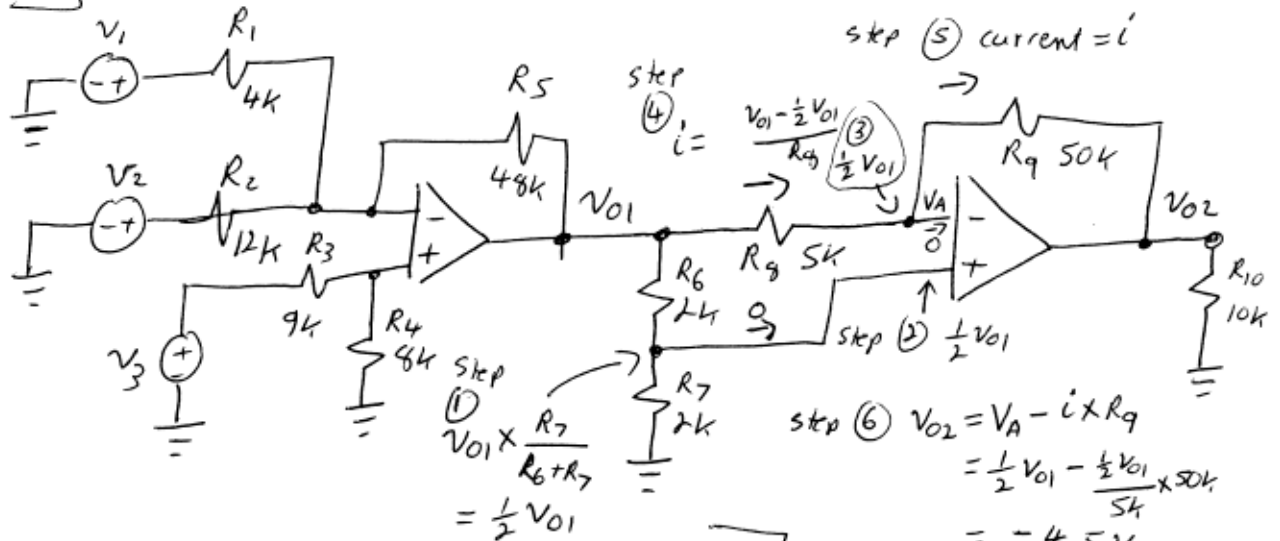
$V_{D2} = V_{on} + i_{D2} R_{on} = 0.8V + 0.092 \times 50 = 0.8 + 4.6V = 5.4V$

Noting breakdown diode:

$\therefore V_{D3} = -5V$



1#6 (a)



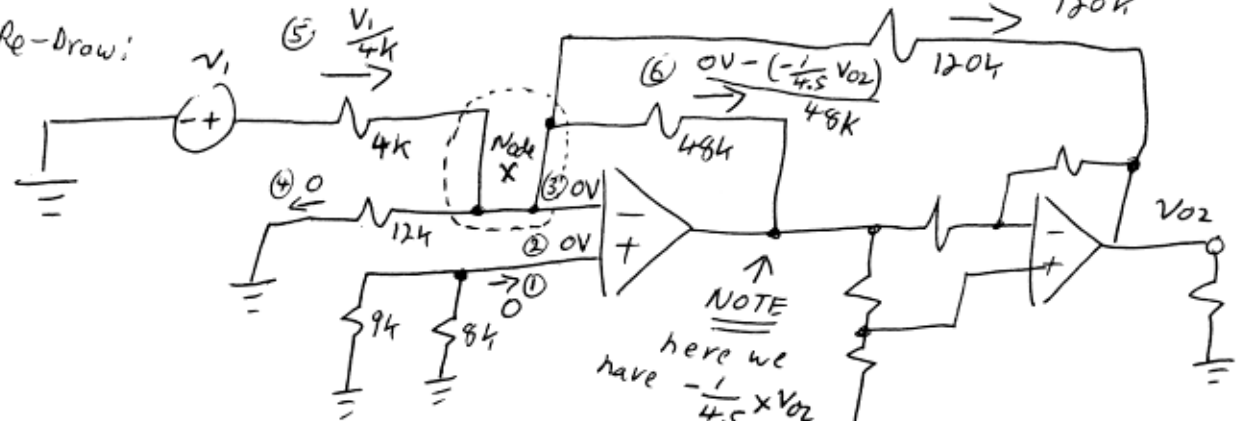
(b) Use superposition with sources v_1, v_2, v_3 .

$v_2=0, v_3=0 \Rightarrow \frac{v_{01}}{v_1} = -\frac{R_5}{R_1} = -\frac{48k}{4k} = -12$
 $v_1=0, v_3=0 \Rightarrow \frac{v_{01}}{v_2} = -\frac{R_5}{R_2} = -\frac{48}{12} = -4$
 $v_1=0, v_2=0 \Rightarrow \frac{v_{01}}{v_3} = \frac{R_4}{R_3+R_4} \times \left(1 + \frac{R_5}{R_1 \parallel R_2}\right) = \frac{8}{17} \times \left(1 + \frac{48}{3}\right) = 8$

Step (7) $\frac{v_{02}}{v_{01}} = -4.5$
 $\therefore \frac{v_{02}}{v_1} = -12 \times (-4.5) = 54$
 $\frac{v_{02}}{v_2} = -4 \times (-4.5) = 18$
 $\frac{v_{02}}{v_3} = 8 \times (-4.5) = -36$

$\therefore v_{02}(t) = 54v_1(t) + 18v_2(t) - 36v_3(t)$

(c) Re-Draw:



KCL at Node X: (5) = (6) + (7)

$$\frac{v_1}{4k} = \frac{1}{48k} \times \frac{1}{4.5} v_{02} - \frac{v_{02}}{120k}$$

$$\frac{v_1}{4k} = v_{02} \left(\frac{1}{216k} - \frac{1}{120k} \right) = -\frac{v_{02}}{270k}$$

$\Rightarrow \frac{v_{02}}{v_1} = -\frac{270}{4} = -67.5$

Note: Parts (a), (b) & (c) could also have been solved with Node Analysis. May 2005 - EPN

22-141 50 SHEETS
 22-142 100 SHEETS
 22-144 200 SHEETS
 PART